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# An ab initio analysis of the electronic structure and harmonic frequencies of nickel porphyrin

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Abstract. Ab initio calculations are performed to understand the geometry, electronic structure, and vibrational frequencies of nickel porphyrin (NiP). Hartree-Fock (HF) and second-order perturbation (MP2) theories are applied with polarized basis sets. The calculated geometrical parameters are in very good agreement with the crystal structure determination. The electronic structure and bonding are analyzed in terms of complexation and correlation effects. Not unexpectedly, the HF depiction of the metal-porphyrin interaction is rather ionic while ligand  $\sigma$  donation is dominant at the MP2 level. Scaled HF frequencies of NiP and its isotopomers are in very good agreement with observed infrared and resonance Raman data.

Key words: Electronic structure  $-$  Harmonic  $frequencies - Nickel porphyrin$ 

# 1 Introduction

Ab initio quantum chemical calculations for small and medium-sized molecules generally yield accurate geometric structures and vibrational frequencies with respect to experimental results. In addition, the computed electronic structure provides qualitative insight into the bonding mechanisms. Software and hardware technologies have advanced to the point where ab initio optimized geometries and harmonic frequencies can be calculated for large transition-metal-containing molecules such as metalloporphyrins.

Metalloporphyrins consist of a macrocyclic tetrapyrrole system with a central metal atom, which may be situated in or above the mean plane of the porphyrin framework. The nature of substituents attached to the porphyrin perimeter can vary the geometric and electronic properties of the complex. Specifically, nonplanarity of the porphyrin framework is induced by steric interactions between bulky substituents, and multiple conformers are possible. The photochemical reactivity of metalloporphyrins is sensitive to the degree of nonplanarity, since excitation can result in geometrical distortions to other stable conformers. The novel conformationally dependent photophysics of nickel porphyrins in particular suggests their possible application as optoelectronic materials. Because of this potentially important use, we examine here the geometry and vibrational frequencies of the parent nickel porphyrin (NiP) (see Fig. 1), with ab initio quantum chemical methods. Our results will be used to guide future computational studies of larger nickel porphyrins.

A brief description of previous ab initio work on freebase porphyrin  $(H_2P)$  which is presumed experimentally to have a delocalized  $D_{2h}$  geometry, provides a useful background to understanding issues relevant to NiP. In the pioneering work of Almlöf et al. on  $H_2P$  [1], it was shown that Hartree-Fock (HF) theory yields a qualitatively incorrect, bond-alternating structure of  $C_{2v}$ symmetry. This is indicated by the presence of two degenerate, low-symmetry, Kekule-type geometries with alternating single and double bonds that have a lower HF energy than the high-symmetry delocalized structure. Expanding the basis set does not eliminate symmetry-breaking, but rather increases the energy separation between the localized and delocalized forms, as well as the degree of bond alteration in the localized structure. However, the overall threshold to symmetrybreaking remains low, e.g., 4.3 kcal/mol with a doubly polarized triple-zeta basis.

Inclusion of electron correlation at the levels of second-order perturbation theory (MP2) or density functional theory (DFT) yields the correct, delocalized  $D_{2h}$ structure [1]. However, the resulting stabilization energy of the  $D_{2h}$  form is quite different by these two methods. Correlation effects in  $H_2P$  were subsequently analyzed in detail by Merchan et al. [2], using complete active space self-consistent field (CASSCF) and CASSCF-based second-order perturbation (CASPT2) methods. Their results support the suitability of the MP2 approach to correlation for  $H_2P$ . The recent development of a new  $H_2P$  force field from scaled DFT force constants by

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Fig. 1. Atom labeling scheme for NiP

Pulay and co-workers [3] is also noteworthy, as it is successful in reproducing experimental frequencies and intensities, and even in suggesting reassignment of some modes. Similar work is in progress for NiP [4].

We recently investigated whether the introduction of a central metal atom is a perturbation sufficient to restore symmetry to the porphyrin framework at the HF level through metal-nitrogen bonding interactions [5]. For NiP, the stable minimum at the HF level is a planar  $C_{2v}$  form, with alternating single and double bonds analogous to the HF minimum found for  $H_2P$ . The delocalized  $D_{4h}$  structure exhibits a pair of imaginary frequencies, corresponding to the expected in-plane distortions towards one or the other bond-alternating geometry. The threshold to symmetry-breaking, however, is much smaller in NiP, e.g., 0.4 kcal/mol at HF/ 6-311G(d). Given this lower threshold relative to  $H_2P$ , it is almost certain that the higher symmetry  $D_{4h}$  structure of NiP is the true minimum upon inclusion of electron correlation.

In this work, we investigate the performance of the HF and MP2 methods in describing the geometry, bonding, and vibrational frequencies for NiP. Although the HF treatment of NiP is limited by a slight symmetrybreaking and a nonquantitative representation of the transition metal-ligand interaction, we find that the HF  $D_{4h}$  geometry and scaled harmonic frequencies are in fact in very satisfactory agreement with experimental measurements. Our HF bonding analysis is also consistent with the empirical four-orbital model developed from spectroscopic data. Finally, we find that the inclusion of electron correlation via MP2 markedly improves the predicted geometry, although frequency evaluation at this level remains prohibitive. The success of the HF method in describing certain aspects of NiP suggests that this level of theory may be applied judiciously to nickel porphyrins with large substituent groups, which presently are not yet tractable at the MP2 level.

## 2 Computational methods

Figure 1 depicts the  $D_{4h}$  structure of NiP and the atom labeling convention  $(C_{\alpha}, C_{\beta}, \text{ and } C_{\text{m}})$  used in this work. The  $C_m$  designation corresponds to meso carbons of the methine bridge while  $C_\beta$  corresponds to the peripheral pyrrole carbons. The x and y axes lie along the  $Ni-N$ bonds, with the z axis out of the center of the porphyrin plane. The Ni 3d orbitals therefore correspond to the following symmetries:  $d_{z^2} = a_{1g}$ ,  $d_{xz} = d_{yz} = d_{\pi} = e_g$ ,  $d_{xy} = b_{2g}$ , and  $d_{x^2-y^2} = b_{1g}$ .

Geometry optimizations and harmonic frequency analyses were performed at the HF level using standard 6-311G and polarized 6-311G(d) basis sets. The latter includes one d function on each C and N, and one f function on Ni. The total numbers of basis functions in our NiP calculations are thus 387 and 514 for the 6- 311G and 6-311G(d) basis sets, respectively. Because of large memory and disk requirements at the MP2 level, we constructed a smaller, general basis set (GBS) for use in these calculations. It consists of 6-311G(d) for Ni, 6-31G(d) for N,  $C_{\alpha}$ , and  $C_{\rm m}$ , and 6-31G for  $C_{\beta}$  and all hydrogens. This GBS basis provides variational flexibility in the central porphyrin region and for the metal at the expense of the outer  $C_{\beta}$ s and hydrogens. Although a compromise, the GBS is shown below to perform as well at the HF level as the larger standard basis sets, yet it totals only 366 functions.

All results were obtained using the multiprocessing Gaussian 94 suite of programs [6] on the Cray C90 and the IBM RS6000 590 cluster at the University of Minnesota and on the SGI Power Challenges at Sandia National Laboratories. Tight thresholds for convergence and geometry optimization were employed throughout. Detailed calculational results, including optimized coordinates and second-derivative matrices, are available from the authors upon request.

## 3 Geometry and energetics

Table 1 lists the HF energy difference between the  $C_{2v}$ minimum and the delocalized  $D_{4h}$  stationary point, and the magnitude of the imaginary  $e_u$  frequency of the  $D_{4h}$ form, for all three basis set employed here. The threshold to HF symmetry-breaking is quite low in NiP compared to  $H_2P$  [5]; it is less than 0.4 kcal/mol for the largest basis set used here, i.e., 6-311G(d). Also, the GBS results reproduce those with the 6-311G(d) basis reasonably well at considerably less computational expense.

Table 2 lists selected optimized geometrical parameters for the  $D_{4h}$  geometry of NiP. Bond lengths calculated for the  $C_{2v}$  minimum [5] bracket the corresponding  $D_{4h}$  distances by about  $\pm 0.003$  Å at the HF/6-311G level, and by  $\pm 0.02$  Å at the HF/6-311G(d) and HF/ GBS levels. Thus, as with the  $C_{2v}$ - $D_{4h}$  energy separation above, bond alternation also increase with increasing

basis set size [5]. The  $C_{\alpha}$ —N— $C_{\alpha}$  bond angle is also listed in Table 2, as for the  $Ni-N$  bond length the bond angles are characteristic markers of the porphyrin core region. Finally, Table 2 lists the results of a single-crystal X-ray diffraction study by Jentzen et al. [7]. This experiment indicates that  $\overrightarrow{NIP}$  is essentially planar  $D_{4h}$ , and this conclusion is supported by both single-crystal and solution-phase resonance Raman spectral analyses [7].

The HF geometrical parameters agree with experimental data to a degree typical for this level of theory applied to transition metal compounds, the expected differences being a  $Ni-N$  distance that is too long and  $N-C_{\alpha}$  distance that is too short. The HF/GBS geometry reproduces closely the HF/6-311G(d) result, with the largest deviation occurring for the  $C_\beta - C_\beta$  bond length. This is not unexpected, since the main deficiency in the GBS basis is for the atoms at the porphyrin periphery. Correlation effects, as accounted for at the  $MP2/GBS$ level, correct the HF deficiencies by decreasing the Ni-N bond length and increasing the N- $C_{\alpha}$  one. The large correlation effect on the  $C_\beta - C_\beta$  bond length is probably an artifact of the smaller basis set used on these atoms. Finally, the  $C_{\alpha}-N-C_{\alpha}$  angle closes down when correlation is included, as the nitrogens are pulled in closer to the metal.

The best agreement with experimental results it obtained at the MP2/GBS level for the core parameters, the Ni-N and N-C<sub> $\alpha$ </sub> bond lengths and the C<sub> $\alpha$ </sub>-N-C<sub> $\alpha$ </sub> bond angle. Of course, the comparison is not ideal since the calculated values correspond to a gas-phase geometry, free of packing forces inherent in the crystal measurement. Note that the GBS is designed to have greater flexibility in the core region, and consequently the MP2-

**Table 1.** Hartree-Fock (HF) energy (kcal/mol) relative to the  $C_{2v}$ minimum and HF  $e_u$  imaginary frequency (cm<sup>-1</sup>) for the  $D_{4h}$ stationary point of NiP

<b>Basis</b>	Relative energy	Imaginary frequency		
$6 - 311G$ $6-311G(d)$ GBS <sup>a</sup>	0.002 0.377 0.186	i87 i799 i657		

<sup>a</sup> General basis set

symmetry

(degree) for NiP and  $P^{-2}$ 

Optimized geometries are also reported for the porphyrin dianion,  $P^{-2}$  (Table 2) to illustrate the porphyrin framework reorganization upon the addition of a central Ni. The bonding interaction between Ni and N, discussed in more detail below, results in a contraction of the  $P^{-2}$  core, with a concomitant decrease in the  $C_{\alpha}$ -N- $C_{\alpha}$ angle. The  $N-C_{\alpha}$  bond is necessarily lengthened by this geometric distortion, while the remaining two  $C_{\alpha}$  bond distances decrease. The perimeter  $C_\beta - C_\beta$  bond length is least affected, being shortened only slightly upon complex formation with Ni.

# 4 Electronic structure and bonding

The electronic structure of NiP can be considered, to a first approximation, as arising from  $Ni<sup>+2</sup>$  inserted into the  $P^{-2}$  complex. In this purely ionic description, i.e., crystal field theory, the Ni adopts a divalent  $d^8$  electronic configuration, with the Ni 4s and  $d_{x^2-y^2}$  orbitals formally empty. The occupation of the remaining 3d orbitals predicted by crystal field theory for  $D_{4h}$  symmetry is  $(e_g)^4 (a_{1g})^2 (b_{2g})^2$ . In metal coordination chemistry, the covalent contribution to the bonding mechanism can then enter as a  $\sigma$  donation from the porphyrin ligand (primarily through the nitrogens) into empty, low-lying Ni orbitals (i.e, the  $d_{x^2-y^2}$  and 4s orbitals). The organometallic  $\pi$  back donation mechanism from metal  $d_{\pi}$ orbitals into ligand-centered  $p_{\pi^*}$  orbitals is less important in NiP given the Ni(II) oxidation state, although the porphyrin has acceptor character owing to its delocalized  $\pi$  network.

Table 3 lists Mulliken populations at the HF and MP2 levels of theory for the GBS basis. A Mulliken population analysis supports the importance of the ionic model at the HF level. The Ni population distribution and total charge of  $+1.5e$  is the same for all three basis sets. The 3*d* population is 8.1e with the individual valence orbital populations calculated as  $d_{xy} = 2.0e$ ,  $d_{xz} = d_{yz} = 2.0e$  each,  $d_{z^2} = 1.9e, d_{x^2-y^2} = 0.2e$ , and  $4s =$ 0.3e, with no significant population in the  $4p$  orbitals. Some degree of  $\sigma$  donation into the Ni  $d_{x^2-y^2}$  orbital is



 $a$  See text for description of general basis set GBS  $\overline{b}$  Ref. [7] X-ray diffraction

<sup>c</sup>Half of the distance between opposite Ns

Table 3. Mulliken population analysis for  $P^{-2}$  and NiP in  $D_{4h}$ symmetry at the  $HF/GBS^a$  and  $MP2/GBS^a$  levels of theory

	HF/GBS <sup>a</sup>			MP2/GBS <sup>a</sup>			
	$\mathbf{P}^{-2}$	$P^{-2}$ @Ni $P^{b}$	NiP	$\mathbf{p}^{-2}$	$P^{-2}(\partial NiP^b)$	<b>NiP</b>	
Ni			1.5			1.2	
N	$-0.5$	$-0.5$	$-1.0$	$-0.4$	$-0.4$	$-0.7$	
$C_{\alpha}$	0.2	0.2	0.3	0.1	0.1	0.1	
	$-0.2$	$-0.2$	$-0.1$	$-0.1$	$-0.1$	$-0.1$	
$\mathcal{C}_{\scriptscriptstyle{\beta}}^{\scriptscriptstyle{\beta}}$	$-0.3$	$-0.3$	$-0.3$	$-0.3$	$-0.3$	$-0.2$	
H	0.1	0.1	0.2	0.1	0.1	0.2	

<sup>a</sup> See text for description of the GBS b  $P^{-2}$  fixed at the geometry of NiP

evident but  $\pi$  back-donation out of Ni  $d_{\pi}$  orbitals is not. Each nitrogen carries a significant negative charge of  $-1.0e$ , while the remaining charge is spread over slightly positive  $C_{\alpha}$  and H atoms, and slightly negative  $C_{\beta}$  and  $C_m$  atoms. Since part of the Ni 4s population is likely owing to the diffuse nature of the highest  $s$  functions in the basis set, even more of the s population should be assigned to nitrogen.

The Mulliken population analysis at the MP2/GBS level favors a more covalent description of the Ni-porphyrin bonding, with the Ni charge reduced to  $+1.2e$ . The 3d population is increased to 8.3e with the individual valence orbital populations calculated as  $d_{xy} = 1.9e$ ,  $d_{xz} = d_{yz} = 2.0e$  each,  $d_{z^2} = 1.9e$ ,  $d_{x^2-y^2} = 0.5e$ , and  $4s =$ 0.5e, with no significant population in the  $4p$  orbitals. A considerable increase in  $\sigma$  donation into the Ni  $d_{x^2-y^2}$ orbital occurs when electron correlation is included, yet  $\pi$  back-donation is still not apparent. Each nitrogen carries a  $-0.7e$  charge which is less than the HF value. The remaining charge is spread over the rest of the atoms in a manner similar to the HF level.

To provide further insight into the metal-porphyrin interaction, a Mulliken population analysis was performed for  $P^{-2}$  at the HF and MP2 levels for the optimized  $D_{4h}$  geometries in Table 2. The calculation was repeated for  $p^{-2}$  fixed at the corresponding  $D_{4h}$  geometry of NiP ( $P^{-2}$ @NiP). Since the HF results are very similar for al three basis sets, only the HF/GBS populations are reported in Table 3, to facilitate comparison with the MP2/GBS results. At both the HF and MP2 levels, the slight distortion of the porphyrin framework to accommodate the central Ni results in negligible changes in the atomic charges between  $P^{-2}$  and  $P^{-2}$  @NiP. The most significant change between  $P^{-2}$ @NiP and NiP is the doubling of the negative charge on nitrogen in the latter. Rather than a consequence of  $d_{\pi}$  backbonding, this is due to small yet cumulative charge redistribution from the rest of the porphyrin framework onto the nitrogens.

The principal character and energies of the important orbitals of NiP are summarized in Table 4. Because of the similarities among all three basis sets, only the HF/6- 311G(d) values are reported. In NiP, the energetic ordering of the Ni d orbitals is  $(b_{2g})^2 (e_g)^4 (a_{1g})^2$ . The dominant charge transfer is due to  $\sigma$  donation from ligand  $a_{1g}$  and  $b_{1g}$  orbitals that can be characterized as primarily nitrogen lone pairs into the formally empty Ni

**Table 4.** Energy (a.u.) and character of pertinent  $D_{4h}$  orbitals of NiP at the HF/6-311G(d) level

Symmetry	Character	Orbital energy		
$b_{2g}$	Pure $3d_{xy}$	$-0.66$		
$e_g$	Primarily $3d_{\pi}$	$-0.60$		
$a_{1q}$	Primarily $3d_{2}$	$-0.57$		
$a_{1q}$	Nitrogen lone pair ( $\sigma$ donation to 4s and $3d_{z^2}$ )	$-0.50$		
$b_{1g}$	Nitrogen lone pair ( $\sigma$ donation to $3d_{x^2-y^2}$ )	$-0.47$		
$a_{2u}$	Ligand $p_{\pi}$ (HOMO-1)	$-0.25$		
$a_{1u}$	Ligand $p_{\pi}$ (HOMO)	$-0.22$		
$e_q$	Ligand $p_{\pi}^*$ $(LUMO, LUMO + 1)$	0.02		

4s and  $d_{x^2-y^2}$ . There is virtually no  $d_{\pi}$  backbonding into the ligand  $e_{g}p_{\pi^*}$  orbitals.

Changes in the nitrogen bond lengths as function of complexation and correlation also contribute to interpreting the bonding mechanism. The magnitude of the bond-length changes from  $P^{-2}$  to NiP are approximately the same between the HF/GBS and MP2/GBS levels, except for the Ni-N bond. There is substantially more contraction of the core region upon NiP formation at the MP2/GBS level, i.e., 0.121 A compared with 0.075 A at the HF/GBS level, demonstrating increased covalent bonding with the inclusion of electron correlation. The  $N-C_{\alpha}$  bond lengthening upon complexation is a geometric consequence of the core contraction, since the porphyrin framework is not that structurally flexible. The remaining bond-length changes from  $p^{-2}$  to NiP are due to the resulting charge redistribution throughout the ligand. The Ni-N bond-length shortening in NiP from the HF/GBS level to the MP2/GBS level is typical of correlation effects on metal-ligand bonds, and supports the increased role of covalent bonding (through  $\sigma$  donation) upon inclusion of correlation.

The electronic interpretation of porphyrin groundstate absorption and excited-state emission is historically described by the qualitative "four-orbital" model of Gouterman [8], which has been validated for  $H_2P$  at the CASPT2 level [2]. In this model, the first two molecular orbitals (MO) are occupied eight-node  $\pi$  MOs of  $a_{2u}$  and  $a_{1u}$  symmetry (HOMO-1, HOMO). There is a clear separation of the nearly degenerate HOMO and HOMO-1 from the rest of the occupied orbitals. The final two orbitals are a degenerate pair of empty ten-node  $\pi$ MOs of  $e_a$  symmetry (LUMO, LUMO+1), which are well-separated from the remaining virtual orbitals.

Within the four-orbital system, the HF orbitals for  $P^{-2}$  conform to the Gouterman model with one minor modification. There is not a large energy separation between the two HOMOs and the remaining filled orbitals. The corresponding four HF orbitals of NiP are very similar to those of  $P^{-2}$ ; however, the HOMOs are now well separated from the remaining filled orbitals as in the Gouterman model. Small contributions also appear from the  $C_{\beta}-C_{\beta} \pi$  bonds to the  $a_{2u}$  HOMO and the  $e_a$  LUMOs.

There are tow previously published DFT studies [9, 10] of NiP, both of which give slightly differing views of the electronic structure based on orbital character, ordering, and Mulliken population analysis. Of course, DFT Mulliken populations are based on orbital constituents of a density and not on orbitals corresponding to a determinantal wavefunction, and the basis set dependence of Mulliken populations precludes any detailed comparison to the results reported here. Both DFT investigations calculate a significantly smaller positive charge on Ni than either HF or MP2 do, but this is due in part to the differences in NiP geometries employed. Also, the DFT descriptions of the HOMO and LUMO consist of 3d orbitals as the primary components, and not the ligand  $p_{\pi}$  orbitals. In contrast, there is no d character in either the HOMO or the LUMO at the HF level or in the four-orbital Gouterman model. For comparative purposes, brief summaries of these DFT results follow.

In the first study, Rosa and Baerends [9] applied nonlocal DFT with a triple-zeta Slater basis set to a nonoptimized NiP geometry, with an assumed  $Ni-N$  bond length of 1.96 Å. They find a Ni total charge of  $+0.6e$ , with a 3d population of 8.6e distributed as  $d_{xy} = 2.0e$ ,  $d_{xz} = d_{yz} = 1.9e$  each,  $d_{z^2} = 1.9e$ ,  $d_{x^2-y^2} = 0.9e$ ,  $4s = 0.4e$ , and  $4p = 0.4e$ ; (note that their paper employs a different axis convention). They conclude that the dominant bonding interaction is due to  $\sigma$  donation from nitrogen lone pairs into the  $d_{x^2-y^2}$  orbital, with additional donation into the 4s and  $4p$  orbitals. The total charge on each nitrogen is -0.6e. Back-donation from  $3d_{\pi}$  to ligand  $p_{\pi^*}$ orbitals and donation from ligand  $p_{\pi}$  into Ni 4p orbitals are negligible. The HOMO is a Ni-centered combination of 4s and  $d_{z^2}$  orbitals, while the LUMO is a mixture of  $d_{x^2-y^2}$  plus nitrogen lone pairs.

In the second study, Matsuzawa et al. [10] employed local DFT with a polarized double-numerical basis set. Their optimized  $Ni-N$  bond length of 1.935 Å is much shorter than the experimental X-ray value, but their remaining bond lengths are in more reasonable agreement. They find a Ni  $3d$  population of 8.7e with the individual valence orbital populations calculated as  $d_{xy} = 2.0e$ ,  $d_{xz} = d_{yz} = 1.9e$  each,  $d_{z2} = 1.9e$ ,  $d_{x2-y2} = 1.0e$ ,  $4s = 0.6e$ , and  $4p = 0.5e$ . This results in a nearly neutral Ni with a total charge of +0.2e. Their HOMO is the degenerate  $d_{\pi}$ orbital and their LUMO is predominantly the  $d_{x^2-y^2}$ orbital.

## 5 Harmonic frequencies

NiP in  $D_{4h}$  symmetry has 105 vibrational modes that transform as  $9a_{1g}$ ,  $9b_{1g}$ ,  $8a_{2g}$ ,  $9b_{2g}$ ,  $18e_u$ ,  $3a_{1u}$ ,  $5b_{1u}$ ,  $6a_{2u}$ ,  $4b_{2u}$ , and  $8eg$  [11]. At the HF level, the  $D_{4h}$  structure of NiP has a degenerate pair of imaginary frequencies of  $e_u$ symmetry, which can subsequently affect the calculated values of the remaining  $e_u$  modes. However, modes of other symmetries should not be strongly affected. In fact, this was successfully demonstrated for  $H_2P$  [12], where HF/3-21G harmonic frequencies of the HF  $D_{2h}$  saddle point reproduced quite well the observed matrix infrared spectra. For NiP, the maximum difference between the non- $e_u$  frequencies of the  $D_{h4}$  form and the corresponding frequencies of the  $C_{2v}$  minimum is only 3 cm<sup>-1</sup> for

the 6-311G basis set. For the GBS and 6-311G(d) basis set, the differences are greater due to the larger geometry changes and larger energy difference between the  $D_{4h}$ and  $C_{2v}$  structures, relative to those of the 6-311G basis. When there is a good correspondence between the nondegenerate modes of the  $D_{4h}$  and  $C_{2v}$  forms, the difference is in the order of  $5-15 \text{ cm}^{-1}$ .

Tables 5 and 6 present scaled HF/6-311G(d) frequencies in comparison to the results of three experimental studies. In the first of these, by Li et al. [13], solution-phase resonance Raman and infrared spectroscopies were used to identify 42 in-plane modes, 15 of which are of  $e_u$  symmetry. The spectra of three deuterated isotopomers of NiP were also measured. The mode labeling used herein is taken directly from this experimental work. A second resonance Raman study by Unger et al. [14] confirms the assignments of Li et al. for 15 modes. The most recent study by Jentzen et al. [7] applied resonance Raman spectroscopy to both singlecrystal and solution forms, and confirms the assignments of six modes from the work of Li et al.

A scaling factor is typically applied to HF frequencies in order to correct for their systematic overestimation owing to the neglect of both electron correlation and anharmonic effects. A standard value of  $0.89$  [15] has been derived from fitting  $HF/6-311G(d)$  frequencies to empirical gas-phase data for molecules not containing transition metals. Since the comparison made here is to solution data, it is reasonable to modify this standard scaling factor to account for solvent effects as well as for the use of the larger  $6-311G(d)$  basis. The best fit to the data of Li et al. [13] is achieved with a uniform scale factor of 0.91.

From Tables 5 and 6, it can be seen that the resulting deviations from the observed fundamentals [13] are typically under 15 cm<sup>-1</sup>, with a few in the range of 20 cm<sup>-1</sup>. The largest differences occur for the lowest  $b_{2q}$  mode and the highest  $a_{2g}$  mode, with an error near  $30^{\circ}$  cm<sup>-1</sup>. The HF/6-311G(d) normal coordinates conform qualitatively with the local coordinate description of Li et al. [13] derived from valence force field calculations. This agreement is strong evidence that the in-plane normal modes of NiP are well understood. Li et al. also assigned 15 inplane  $e_u$  modes, but the use of  $D_{4h}$  frequencies precludes comparison to the scaled HF values, for the reason discussed above. Apart from the imaginary  $e_u$  mode which correlates with in-plane N- $C_{\alpha}$ ,  $C_{\alpha}-C_{\beta}$ , and  $C_{\alpha}-C_{\beta}$ stretching toward the bond-alternating  $C_{2v}$  geometry, however, the agreement with the remaining observed  $e_u$ modes is actually quite satisfactory.

Isotopic frequencies were computed for NiP with deuteriums replacing hydrogens bonded to the  $C_{\alpha}$ ,  $C_{\beta}$ , and  $C_{\alpha}$  +  $C_{\beta}$  carbons (labeled NiP-d<sub>4</sub>, d<sub>8</sub>, and d<sub>12</sub>, respectively), and then scaled uniformly by 0.91. The results for these isotopomers are listed in Tables 5 and 6, and the experimental isotope effects are well reproduced. The average magnitude of the deviation from the observed fundamentals is  $17 \text{ cm}^{-1}$ . There are a few instances where the disagreement is much larger, but the only egregious one is the 75 cm<sup>-1</sup> difference for the  $v_{26}$  mode in NiP- $d_{12}$ . In this case, the experimental band at 848 cm<sup>-1</sup> is attributed to both the  $a_{2g}$  mode  $v_{26}$  and the

	NiP					$NiP-d_4$		$NiP-d_8$		$NiP-d_{12}$	
	$\mathbf{HF}^{\text{a}}$	Expt. <sup>b</sup>	Expt. <sup>c</sup>	Expt. <sup>d</sup>	HF <sup>a</sup>	Expt. <sup>b</sup>	$\mathbf{HF}^{\text{a}}$	Expt. <sup>b</sup>	$\mathbf{HF}^{\text{a}}$	Expt. <sup>b</sup>	
$a_{1g}$											
v <sub>5</sub>	3104				3103		2318		2318		
$v_1$	3061				2263		3061		2263		
$v_2$	1587	1574	1572	1575; 1576	1581	1566	1559	1552	1550	1546	
$v_3$	1465	1459			1458	1456	1442	1431	1439	1427	
$v_4$	1390	1376	1376	1377;1378	1390	1374	1379	1367	1379	1367	
$v_{9}$	1075	1066	1065		1075	1065	778	775	777	773	
$v_6$	995	995	994		992	992	986	987	985	985	
$v_7$	725	732			703	711	722	720	701	709	
$v_8$	351	369			350	367	344	360	343	359	
$b_{1g}$											
$v_{14}$	3103				3103		2317		2317		
$v_{10}$	1628	1650	1648	1651; 1651	1613	1642	1625	1646	1609	1636	
$v_{11}$	1525	1505	1502		1522	1504	1471	1454	1465	1454	
$v_{12}$	1408				1344	1321	1405	1324	1344	1315	
$v_{13}$	1198	1185	1184		958	938	1193	1179	964	948	
$v_{17}$	1067	1060	1058		1087		803	768	773	768	
$v_{15}$	997	1003	1002		1007	1020	981		1012		
$v_{16}$	734	732			668	665	707	705	661	655	
$v_{18}$	216	237			216	237	212	232	212	232	

**Table 5.** Scaled<sup>a</sup>  $a_{1g}$  and  $b_{1g}$  HF/6-311G(d) frequencies (cm<sup>-1</sup>) for the  $D_{4h}$  structure of NiP, with corresponding observed fundamentals for NiPb,c,d and its isotopomers<sup>b</sup>

a Scaled by 0.91; see text for details<br>
b Ref. [13] infrared and resonance Raman solution data<br>
c Ref. [14] resonance Raman solution data<br>
d Ref. [7] first value from resonance Raman single-crystal data and second value fr

	NiP			$NiP-d_4$		$NiP-d_8$		$NiP-d_{12}$		
	HF <sup>a</sup>	Expt. <sup>b</sup>	Expt. <sup>c</sup>	Expt. <sup>d</sup>	$\mathbf{HF}^{\text{a}}$	Expt. <sup>b</sup>	$\mathbf{HF}^{\text{a}}$	Expt. <sup>b</sup>	HF <sup>a</sup>	Expt. <sup>b</sup>
$a_{2g}$										
$v_{23}$	3083				3083		2278		2278	
$v_{19}$	1582	1611	1603	1608; 1606	1557	1598	1579	1605	1551	1592
$v_{20}$	1371	1354			1358	1347	1331	1313	1298	1278
$v_{26}$	1331	1317	1315	1317; 1317	1284	1249	854	851	923	848
$v_{21}$	1162	1139	1137		925	910	1265	1256	847	848
$v_{22}$	1006	1005	1003		1010	1012	1118	1095	1204	1189
$v_{24}$	796	806			775	783	777	788	761	767
$v_{25}$	420	429			410	419	398	404	389	397
$b_{2g}$										
$v_{31}$	3083				3083		2278		2279	
$v_{27}$	3060				2262		3061		2261	
$v_{28}$	1502	1505			1497	1477	1482	1487	1475	1481
$v_{29}$	1383	1368	1354	1355; 1356	1380	1368	1343	1324	1343	1315
$v_{34}$	1198	1193	1193		1197	1193	971		965	948
$v_{30}$	1063				1047	1020	1086		1072	
$v_{32}$	824	819			814	815	770	799	764	780
$v_{33}$	415	435			415	432	381	399	381	399
$v_{35}$	228	197			224	197	226	197	223	197

**Table 6.** Scaled<sup>a</sup>  $a_{2g}$  and  $b_{2g}$  HF/6-311G(d) frequencies (cm<sup>-1</sup>) for the  $D_{4h}$  structure of NiP, with corresponding observed fundamentals for NiPb,c,d and its isotopomers<sup>b</sup>

<sup>a</sup> Scaled by 0.91; see text for details<br>
<sup>b</sup> Ref. [13] infrared and resonance Raman solution data<br>
<sup>c</sup> Ref. [14] resonance Raman solution data<br>
<sup>d</sup> Ref. [7] first value from resonance Raman single-crystal data and second

 $a_{2g}$  mode  $v_{21}$ . This assignment seems rather unlikely based on the present HF results.

The remaining modes of  $a_{1u}$ ,  $b_{1u}$ ,  $a_{2u}$ ,  $b_{2u}$ , and  $e_g$ symmetry correspond to out-of-plane distortions categorized  $[16]$  as propeller (pro), ruffle (ruf), dome (dom), saddle (sad), and wave (wav), respectively (Table 7). The lowest modes of each symmetry can be described as follows. The  $a_{1u}$  propeller mode has each pyrrole ring twisted in the same direction about its  $Ni-\overline{N}$  bond. The  $b_{1u}$  ruffling mode is similar to the propeller motion but

Table 7. Scaled<sup>a</sup> HF/6-311G(d) frequencies  $(cm^{-1})$  for the  $D_{4h}$ structure of NiP, for symmetries  $a_{1u}$ ,  $b_{1u}$ ,  $a_{2u}$ , and  $e_g$ . The out-ofplane distortions are categorized as propeller (pro), ruffle (ruf), dome (dom), saddle (sad), and wave (wav)

$a_{1u}$ (pro)	$b_{1\mu}$ (ruf)	$a_{2u}$ (dom)	$b_{2\mu}$ (sad)	$e_q$ (wav)
938 688 289	944 864 703 474 52	885 797 729 355 257 93	816 682 249 52	942 875 805 718 678 434 216 152

<sup>a</sup> Scaled by 0.91, see text for details

with alternate pyrrole rings twisted in opposite directions about their Ni-N bonds. The  $a_{2u}$  doming mode has the central Ni and the nitrogens pulled up from the mean plane of the porphyrin framework, with the beta carbons pulled down. The  $b_{2u}$  saddling mode consists of alternate pyrrole rings displaced up or down while the meso carbons remain in the mean plane. The degenerate  $e_a$  waving mode has one pair of opposing pyrrole rings displaced up and down, while the other pair are twisted in the same direction about their Ni-N bonds.

The out-of-plane vibrations that are either IR or Raman active have not yet been experimentally measured. Table 7 reports scaled HF/6-311G(d) values for these frequencies, which are sensitive to nonplanar conformations in substituted nickel porphyrins where steric interactions induce a variety of types and degrees of nonplanarity. The results in Table 7 will therefore be relevant to future theoretical studies that examine substituent effects in metalloporphyrins. For larger functionalized nickel porphyrins, of course, HF harmonic frequency determinations are feasible only with smaller basis sets.

#### 6 Summary

The HF description of NiP suffers from a symmetrybreaking artifact, albeit with a very low energy difference of 0.4 kcal/mol between the  $C_{2v}$  minimum and the localized  $D_{4h}$ -stationary point. The  $D_{4h}$  geometry is in satisfactory agreement with a recent crystal structure determination, i.e., within the expected degree of accuracy for transition metal-ligand bonding at the HF level. Accounting for electron correlation effects at the MP2 level considerably improves the agreement with experiment.

The Ni  $d_{x^2-y^2}$  orbital, which is formally empty in an ionic description of the bonding, is moderately populated at the HF level due to  $\sigma$  donation from nitrogen lone pairs on the ligand. However, the HF description of the Ni-porphyrin interaction remains rather ionic. With the inclusion of correlation at the MP2 level,  $\sigma$  donation is notably enhanced and is the dominant bonding mechanism. There is little evidence fof  $\pi$  backbonding at

either the HF of MP2 levels. The historical "fourorbital'' model of Gouterman is validated for NiP and the dianion  $P^{-2}$ . The HOMOs and LUMOs consist of ligand  $p_{\pi}$ -centered orbitals, in contrast to earlier DFT predictions of considerable Ni 3d character in these orbitals.

Harmonic frequencies computed at the HF level and uniformly scaled compare quite well with observed inplane IR and resonance Raman data of NiP and its isotopomers. This satisfactory level of agreement suggests that scaled HF frequencies may be adequate for nickel porphyrins with large substituent groups. Frequencies are also reported for out-of-plane vibrations, as these will provide the key in future studies of substituted nickel porphyrins, where multiple nonplanar conformations are possible.

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